

RAZDALJA MED DVEMA TOČKAMA V RAVNINI

RAZDALJA MED TOČKAMA $A(x_1, y_1)$ IN $B(x_2, y_2)$:

$$d(A, B) = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

1. Izračunaj razdaljo med točkama.



a) $A(3, -2)$ in $B(5, 7)$
 $x_1 \quad y_1 \quad x_2 \quad y_2$

$$d(A, B) = \sqrt{(5-3)^2 + (7-(-2))^2} = \sqrt{2^2 + 9^2} = \sqrt{4 + 36} = \sqrt{40} = \underline{\underline{2\sqrt{10}}}$$

b) $C(-4, -7)$ in $D(6, -8)$
 $x_1 \quad y_1 \quad x_2 \quad y_2$

$$d(C, D) = \sqrt{(6-(-4))^2 + (-8-(-7))^2} = \sqrt{10^2 + (-1)^2} = \sqrt{100 + 1} = \underline{\underline{\sqrt{101}}}$$

c) $E(\sqrt{6}, 4)$ in $F(7, -\sqrt{6})$
 $x_1 \quad y_1 \quad x_2 \quad y_2$

$$\begin{aligned} d(E, F) &= \sqrt{(7-\sqrt{6})^2 + (-\sqrt{6}-4)^2} = \sqrt{49 - 14\sqrt{6} + 6 + 6 + 8\sqrt{6} + 16} = \\ &= \underline{\underline{\sqrt{77 - 6\sqrt{6}}}} \end{aligned}$$

d) $G(0,9, -3,4)$ in $H(4,5, -0,3)$
 $x_1 \quad y_1 \quad x_2 \quad y_2$

$$d(G, H) = \sqrt{(4,5-0,9)^2 + (-0,3-(-3,4))^2} = \sqrt{3,6^2 + 3,1^2} = \sqrt{22,57} = \underline{\underline{4,75}}$$

2. Pokaži, da je trikotnik z oglišči $A(-16,0)$, $B(-2,6)$ in $C(-6,-4)$ pravokoten.

v pravokotnem trikotniku velja Pitagorov izrek: $c^2 = a^2 + b^2$

Izračunaj $d(A,B)$, $d(A,C)$ in $d(B,C)$

$A(-16,0)$, $B(-2,6)$

$$d(A,B) = \sqrt{(-2 - (-16))^2 + (6 - 0)^2} = \sqrt{14^2 + 6^2} = \sqrt{232} = 2\sqrt{58} \text{ - hipotenuza (najdaljša)}$$

$A(-16,0)$, $C(-6,-4)$

$$d(A,C) = \sqrt{(-6 + 16)^2 + (-4 + 0)^2} = \sqrt{10^2 + (-4)^2} = \sqrt{116} = 2\sqrt{29}$$

$B(-2,6)$, $C(-6,-4)$

$$d(B,C) = \sqrt{(-6 + 2)^2 + (-4 - 6)^2} = \sqrt{(-4)^2 + (-10)^2} = \sqrt{116} = 2\sqrt{29}$$

$$c^2 = a^2 + b^2$$

$$(2\sqrt{58})^2 = (2\sqrt{29})^2 + (2\sqrt{29})^2$$

$$232 = 116 + 116 \quad \checkmark \quad \text{je pravokoten.}$$



3. Izračunaj obseg trikotnika z oglišči $A(-3,2)$, $B(5,17)$, $C(8,13)$.

izračunaj dolžine vseh stranic in jih sešteješ

$$\sigma = d(A,B) + d(A,C) + d(B,C)$$

$A(-3,2)$, $B(5,17)$

$$d(A,B) = \sqrt{(5 + 3)^2 + (17 - 2)^2} = \sqrt{8^2 + 15^2} = \sqrt{289} = 17$$

$A(-3,2)$, $C(8,13)$

$$d(A,C) = \sqrt{(8 + 3)^2 + (13 - 2)^2} = \sqrt{11^2 + 11^2} = \sqrt{242} = 11\sqrt{2}$$

$B(5,17), C(8,13)$

$$d(B,C) = \sqrt{(8-5)^2 + (13-17)^2} = \sqrt{3^2 + (-4)^2} = \sqrt{25} = 5$$

$$\sigma = 17 + 11\sqrt{2} + 5 = \underline{\underline{22 + 11\sqrt{2}}}$$

4. Na ordinatni osi poišči točko, ki je enako oddaljena od točk $A(3,1)$ in $B(-1,5)$.

na ordinatni (y) osi: $T(0, y)$

$$d(A,T) = d(B,T)$$

$$d(A,T) = \sqrt{(0-3)^2 + (y-1)^2} = \sqrt{(-3)^2 + y^2 - 2y + 1} = \sqrt{y^2 - 2y + 10}$$

$$d(B,T) = \sqrt{(0+1)^2 + (y-5)^2} = \sqrt{1 + y^2 - 10y + 25} = \sqrt{y^2 - 10y + 26}$$

enačis

$$\sqrt{y^2 - 2y + 10} = \sqrt{y^2 - 10y + 26} \quad /^2$$

$$y^2 - 2y + 10 = y^2 - 10y + 26$$

$$8y = 16 \quad /: 8$$

$$y = 2$$

$$\underline{\underline{T(0,2)}}$$



5. Na abscisni osi poišči točko, ki je enako oddaljena od točk $A(\sqrt{3}, -1)$ in $B(0, \sqrt{13})$.

na abscisni (x) osi: $T(x, 0)$

$$d(A,T) = d(B,T)$$

$$d(A,T) = \sqrt{(x-\sqrt{3})^2 + (0+1)^2} = \sqrt{x^2 - 2\sqrt{3}x + 3 + 1} = \sqrt{x^2 - 2\sqrt{3}x + 4}$$

$$d(B,T) = \sqrt{(x-0)^2 + (0-\sqrt{13})^2} = \sqrt{x^2 + (-\sqrt{13})^2} = \sqrt{x^2 + 13}$$

enačis

$$\sqrt{x^2 - 2\sqrt{3}x + 4} = \sqrt{x^2 + 13} \quad /^2$$

$$\cancel{x^2} - 2\sqrt{3}x + 4 = \cancel{x^2} + 13$$

$$-2\sqrt{3}x = 9$$

$$x = -\frac{3\sqrt{3}}{2}$$

$$\underline{\underline{T\left(-\frac{3\sqrt{3}}{2}, 0\right)}}$$



6. Točka $T(a+1, 2-a)$ je enako oddaljena od točk $A(-2, 2)$ in $B(4, -1)$.
Izračunaj a .

$$A(-2, 2), B(4, -1), T(a+1, 2-a)$$

$$d(A, T) = d(B, T)$$

$$d(A, T) = \sqrt{(a+1+2)^2 + (2-a-2)^2} = \sqrt{(a+3)^2 + (-a)^2} = \sqrt{a^2 + 6a + 9 + a^2} = \sqrt{2a^2 + 6a + 9}$$

$$d(B, T) = \sqrt{(a+1-4)^2 + (2-a+1)^2} = \sqrt{(a-3)^2 + (3-a)^2} = \sqrt{a^2 - 6a + 9 + 9 - 6a + a^2} = \sqrt{2a^2 - 12a + 18}$$

$$\sqrt{2a^2 + 6a + 9} = \sqrt{2a^2 - 12a + 18} \quad /^2$$

$$\cancel{2a^2} + 6a + 9 = \cancel{2a^2} - 12a + 18$$

$$18a = 9 \quad /: 18$$

$$\underline{\underline{a = \frac{1}{2}}}$$